What is claimed is:

1	. In a communication network comprising an ingress node, a
2	plurality of core nodes connected by links to the ingress node, and an egress
3	node connected by links to the ingress node via the core nodes, said ingress
4	node receiving communication traffic of the network and said egress node
5	delivering communication traffic of the network, an apparatus for designing a
6	plurality of communication paths between said ingress node and said egress
7	node, the apparatus comprising:
8	means for defining an objective function for minimizing a number of
9	candidate tree graphs for accommodating said communication paths;
10	means for defining a first constraint equation for causing all of said
11	candidate tree graphs to form a tree;
12	means for defining a second constraint equation for accommodating said
13	communication paths in one of said candidate tree graphs;
14	means for defining a third constraint equation for determining whether
15	each of said candidate tree graphs is used to accommodate said communication
16	paths; and
17	means for solving a mathematical programming problem formed by said
18	objective function, and said first, second and third constrain equations to
19	obtain a plurality of trees in which said communication paths can be
20	accommodated.

- In a communication network comprising an ingress node, a
- 2 plurality of core nodes connected by links to the ingress node, and an egress

accommodated.

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- node connected by links to the ingress node via the core nodes, said ingress node receiving communication traffic of the network and said egress node 4 delivering communication traffic of the network, an apparatus for designing a 5 plurality of communication paths between said ingress node and said egress 6 node, the apparatus comprising: 7 means for storing an existing tree and determining whether said 8 communication paths can be accommodated in said existing tree; 9 10 means for defining an objective function for minimizing a number of candidate tree graphs for accommodating ones of said communication paths 11 which cannot be accommodated in said existing tree; 12 13 means for defining a first constraint equation for causing all of said 14 candidate tree graphs to form a tree if all of said communication paths cannot be accommodated in said existing tree; 15 16 means for defining a second constraint equation for accommodating said ones of communication paths in one of said candidate tree graphs; 17 means for defining a third constraint equation for determining whether 18 19 each of said candidate tree graphs is used to accommodate at least one of said communication paths; and 20 means for solving a mathematical programming problem formed by said 21 objective function, and said first, second and third constrain equations to 22 23 obtain a plurality of trees in which said ones of communication paths can be
  - In a communication network comprising an ingress node, a plurality of core nodes connected by links to the ingress node, and an egress

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- 3 node connected by links to the ingress node via the core nodes, said ingress
- 4 node receiving communication traffic of the network and said egress node
- 5 delivering communication traffic of the network, an apparatus for designing a
- 6 plurality of communication paths between said ingress node and said egress
- 7 node, the apparatus comprising:
- 8 means for defining a first constraint equation for causing all candidate
- 9 tree graphs to form a tree;
- means for defining a second constraint equation for accommodating said
- 11 communication paths in one of said candidate tree graphs;
- means for embedding non-negative artificial variables into said first and
- 13 second constraint equations;
- means for defining an objective function for minimizing a total number
- of said non-negative artificial variables; and
- means for solving a mathematical programming problem formed by said
- objective function, and said first and second constrain equations to obtain a
- 18 plurality of trees in which said communication paths can be accommodated.
- In a communication network comprising an ingress node, a
- 2 plurality of core nodes connected by links to the ingress node, and an egress
- 3 node connected by links to the ingress node via the core nodes, said ingress
- 4 node receiving communication traffic of the network and said egress node
- 5 delivering communication traffic of the network, an apparatus for designing a
- 6 plurality of communication paths between said ingress node and said egress
- 7 node, the apparatus comprising:
- 8 means for storing an existing tree and determining whether said

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9	communication paths can be accommodated in said existing tree;
10	means for defining a first constraint equation for accommodating ones
11	of said communication paths which cannot be accommodated in said existing
12	tree in one of said candidate tree graphs;
13	means for defining a second constraint equation for causing all of said
14	candidate tree graphs to form a tree;
15	means for embedding non-negative artificial variables into said first and
16	second constraint equations;
17	means for defining an objective function for minimizing a total number
18	of said non-negative artificial variables; and
19	means for solving a mathematical programming problem formed by
20	said objective function, and said first and second constrain equations to
21	obtain a plurality of trees in which said ones of communication paths can be
22	accommodated.
1	In a communication network comprising an ingress node, a

In a communication network comprising an ingress node, a

plurality of core nodes connected by links to the ingress node, and an egress

node connected by links to the ingress node via the core nodes, said ingress

node receiving communication traffic of the network and said egress node

delivering communication traffic of the network, a method of designing a

plurality of communication paths between said ingress node and said egress

node, the method comprising:

defining an objective function for minimizing a number of candidate to

defining an objective function for minimizing a number of candidate tree graphs for accommodating said communication paths;

defining a first constraint equation for causing all of said candidate tree

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11	graphs to form a tree;
12	defining a second constraint equation for accommodating said
13	communication paths in one of said candidate tree graphs;
14	defining a third constraint equation for determining whether each of
15	said candidate tree graphs is used to accommodate said communication paths;
16	and
17	solving a mathematical programming problem formed by said objective
18	function, and said first, second and third constrain equations to obtain a
19	plurality of trees in which said communication paths can be accommodated.
1	In a communication network comprising an ingress node, a
2	plurality of core nodes connected by links to the ingress node, and an egress
3	node connected by links to the ingress node via the core nodes, said ingress
4	node receiving communication traffic of the network and said egress node
5	delivering communication traffic of the network, a method of designing a
6	plurality of communication paths between said ingress node and said egress
7	node, the method comprising:
8	storing an existing tree and determining whether said communication
9	paths can be accommodated in said existing tree;
10	defining an objective function for minimizing a number of candidate tree
11	graphs for accommodating ones of said communication paths which cannot be
12	accommodated in said existing tree;
13	defining a first constraint equation for causing all of said candidate tree
14	graphs to form a tree if all of said communication paths cannot be
15	accommodated in said existing tree;

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16	defining a second constraint equation for accommodating said ones of
17	communication paths in one of said candidate tree graphs;
18	defining a third constraint equation for determining whether each of
19	said candidate tree graphs is used to accommodate at least one of said
20	communication paths; and
21	solving a mathematical programming problem formed by said objective
22	function, and said first, second and third constrain equations to obtain a
23	plurality of trees in which said ones of said communication paths can be
24	accommodated.
1	In a communication network comprising an ingress node, a
2	plurality of core nodes connected by links to the ingress node, and an egress
3	node connected by links to the ingress node via the core nodes, said ingress
4	node receiving communication traffic of the network and said egress node
5	delivering communication traffic of the network, a method of designing a
6	plurality of communication paths between said ingress node and said egress
7	node, the method comprising:
8	defining a first constraint equation for causing all candidate tree graphs
9	to form a tree;
10	defining a second constraint equation for accommodating said
11	communication paths in one of said candidate tree graphs;
12	embedding non-negative artificial variables into said first and second
13	constraint equations;
14	defining an objective function for minimizing a total number of said
15	non-negative artificial variables, and

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16 solving a mathematical programming problem formed by said objective function, and said first and second constrain equations to obtain a plurality of 17 trees in which said communication paths can be accommodated. 18

₿. In a communication network comprising an ingress node, a 1 plurality of core nodes connected by links to the ingress node, and an egress 2 node connected by links to the ingress node via the core nodes, said ingress 3 node receiving communication traffic of the network and said egress node 4 delivering communication traffic of the network, a method of designing a 5 plurality of communication paths between said ingress node and said egress 6 node, the method comprising: 7 8 storing an existing tree and determining whether said communication 9 paths can be accommodated in said existing tree; 10 defining a first constraint equation for accommodating ones of said communication paths which cannot be accommodated in said existing tree in 11 one of said candidate tree graphs; 12 defining a second constraint equation for causing all of said candidate 13 14 tree graphs to form a tree; embedding non-negative artificial variables into said first and second 15 constraint equations; 16 17 defining an objective function for minimizing a total number of said non-negative artificial variables; and 18 solving a mathematical programming problem formed by said objective 19 function, and said first and second constrain equations to obtain a plurality of 20 trees in which said ones of communication paths can be accommodated.

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In a communication network comprising an ingress node, a 1 plurality of core nodes connected by links to the ingress node, and an egress 2 node connected by links to the ingress node via the core nodes, said ingress 3 node receiving communication traffic of the network and said egress node 4 delivering communication traffic of the network, a storage medium for storing 5 an algorithm for operating a computer to design a plurality of communication 6 paths between said ingress node and said egress node, said algorithm 7 comprising: 8 defining an objective function for minimizing a number of candidate tree 9 10 graphs for accommodating said communication paths; defining a first constraint equation for causing all of said candidate tree 11 graphs to form a tree; 12 13 defining a second constraint equation for accommodating said communication paths in one of said candidate tree graphs; 14 15 defining a third constraint equation for determining whether each of said candidate tree graphs is used to accommodate said communication paths; 16 and 17 18 solving a mathematical programming problem formed by said objective function, and said first, second and third constrain equations to obtain a 19 plurality of trees in which said communication paths can be accommodated. 20

1 W. In a communication network comprising an ingress node, a
2 plurality of core nodes connected by links to the ingress node, and an egress
3 node connected by links to the ingress node via the core nodes, said ingress
4 node receiving communication traffic of the network and said agrees and

node receiving communication traffic of the network and said egress node

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- delivering communication traffic of the network, a storage medium for storing an algorithm for operating a computer to design a plurality of communication 6 paths between said ingress node and said egress node, said algorithm 7 8 comprising: storing an existing tree and determining whether said communication 9 paths can be accommodated in said existing tree; 10 defining an objective function for minimizing a number of candidate tree 11 graphs for accommodating ones of said communication paths which cannot be 12 accommodated in said existing tree; 13 defining a first constraint equation for causing all of said candidate tree 14 graphs to form a tree if all of said communication paths cannot be 15 16 accommodated in said existing tree; defining a second constraint equation for accommodating said ones of 17 communication paths in one of said candidate tree graphs; 18 defining a third constraint equation for determining whether each of 19 said candidate tree graphs is used to accommodate at least one of said 20 21 communication paths; and solving a mathematical programming problem formed by said objective 22 function, and said first, second and third constrain equations to obtain a 23
- In a communication network comprising an ingress node, a
  plurality of core nodes connected by links to the ingress node, and an egress
  node connected by links to the ingress node via the core nodes, said ingress
  node receiving communication traffic of the network and said egress node

plurality of trees in which said communication paths can be accommodated.

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- delivering communication traffic of the network, a storage medium for storing 5 an algorithm for operating a computer to design a plurality of communication paths between said ingress node and said egress node, said algorithm 7 comprising: 8 defining a first constraint equation for causing all candidate tree graphs 9 to form a tree; 10 defining a second constraint equation for accommodating said 11 communication paths in one of said candidate tree graphs; 12 embedding non-negative artificial variables into said first and second 13 14 constraint equations; defining an objective function for minimizing a total number of said 15 16 non-negative artificial variables; and solving a mathematical programming problem formed by said objective 17 function, and said first and second constrain equations to obtain a plurality of 18
- 1 12. In a communication network comprising an ingress node, a
  2 plurality of core nodes connected by links to the ingress node, and an egress
  3 node connected by links to the ingress node via the core nodes, said ingress
  4 node receiving communication traffic of the network and said egress node
  5 delivering communication traffic of the network, a storage medium for storing
  6 an algorithm for operating a computer to design a plurality of communication
  7 paths between said ingress node and said egress node, said algorithm
  8 comprising:

trees in which said ones of said communication paths can be accommodated.

9 storing an existing tree and determining whether said communication

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10	partis carrie accommodated in said existing tree;
11	defining a first constraint equation for accommodating ones of said
12	communication paths which cannot be accommodated in said existing tree in
13	one of said candidate tree graphs;
14	defining a second constraint equation for causing all of said candidate
15	tree graphs to form a tree;
16	embedding non-negative artificial variables into said first and second
17	constraint equations;
18	defining an objective function for minimizing a total number of said
19	non-negative artificial variables; and
20	solving a mathematical programming problem formed by said objective
21	function, and said first and second constrain equations to obtain a plurality of
22	trees in which said ones of communication paths can be accommodated.